

# Vehicle Propulsion Systems

## Lecture 1

### Course Introduction & Energy System Overview

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## Outline

About the Course

More Course Details

Analyzing Energy Demand for a Vehicle

Energy Consumption of a Driving Mission

The Vehicle Motion Equation

Losses in the vehicle motion

Energy Demand of Driving Missions

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## Vehicle Propulsion Systems

Vehicles as a hot topic is everlasting

- ▶ Brings freedom to the user
- ▶ Have a direct influence on the environment
- ▶ Consume resources that are limited
- ▶ Have different appeal to different persons



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## Vehicle Propulsion Systems

A diversity of powertrain configurations is appearing

- ▶ Conventional Internal Combustion Engine (ICE) powertrain. Diesel, Gasoline, New concepts
- ▶ Hybrid powertrains – Parallel/Series/Complex configurations
- ▶ Fuel cell electric vehicles
- ▶ Electric vehicles

Course goal:

- ▶ Introduction to powertrain configuration and optimization problems
- ▶ Mathematical models and ...
- ▶ ... methods for
  - ▶ Analyzing powertrain performance
  - ▶ Optimizing the powertrain energy consumption

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## Top Priorities in Vehicle Development

- ▶ Improve the fuel economy of vehicles (Better cars are our best oil-wells)
- ▶ Reduce costs
- ▶ Drivability
- ▶ Safety
- ▶ Emissions
  - ▶ Exhaust emissions
  - ▶ Road dust
  - ▶ Noise
  - ▶ Legislations

All issues are important but the first item is the main topic here.

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## Vehicle properties

The vehicle in focus is passenger cars. (In the book.)

–What characterizes passenger cars?

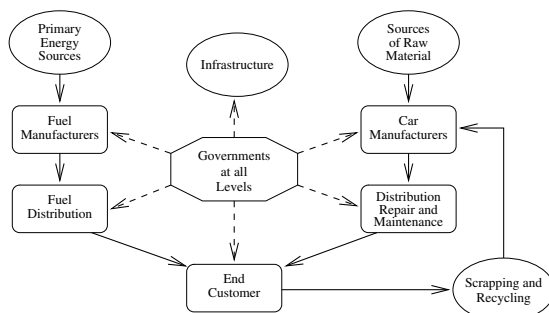
- ▶ Autonomous and do not depend on fixed power grid.
- ▶ Have refueling time negligible compared to the driving time between two refuelings.
- ▶ Transport two to six persons and some payload.
- ▶ Accelerate from 0 to 100 km/h in 10-15 seconds, or drive uphill a 5% ramp at legal top speed.

Methods and tools are also applicable to trucks and other transportation systems.

- ▶ Numerical values differ
- ▶ Demands are different
- ▶ Principles are the same but solutions differ

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## Life Cycle of a Vehicle



Many things are important!

–Focus is on energy path and in-vehicle energy conversion

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## Examination – 5 (3) Hand-In Assignments

Hand-In assignments done **individually**.  
Compendium for Hand-In assignments.

- Fuel consumption requirement of a driving mission.  
Methods and tools for estimating the fuel consumption.  
–Mandatory and optional tasks.
- Optimal control of series and hybrid concepts.  
Tools for investigating the best possible driving schedule.  
–Mandatory and optional tasks.
- ECMS based on-line control of a parallel hybrid.  
Standard optimal control based controller.  
–Mandatory and optional tasks.
- Three concepts for short term energy storage.  
Very open ended problems.  
–Optional tasks.
- Fuel cell vehicle.  
–Optional tasks.

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## Examination – Grading system

- Pass – Grade 3.  
All mandatory tasks must be completed.  
Handed in, examined, returned (corrected, handed in again, until pass).
- Higher grades.  
Handed in, graded by us (like an exam), returned.  
Point system connected to extra tasks.
  - ▶ Grade 3 – 0-13 p
  - ▶ Grade 4 – 14-? p
  - ▶ Grade 5 – 24-? p
- More details are found in the project PM.  
Deadlines given on the home page and Lisam.

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## Resources

- ▶ Computer tools are necessary, to be able to solve interesting problems.  
–Matlab and Simulink with extra packages.
- ▶ If you have your own computer, we encourage you to use it.
- ▶ 4 computer room booked on 2 occasions per week  
Tue 13–17, and Thursday 8–10 (Wed 17–21, Fri 13–17).
- ▶ See it as support opportunity.
  - Lab room assistant, answers questions.
  - Collect your questions and come to us.

Preparations for hand-in – Refresh your knowledge  
Matlab and Simulink programming experience.

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## Course Outline

Let's have a look at Lisam! Let's have a look at the course home page!

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## Outline

About the Course

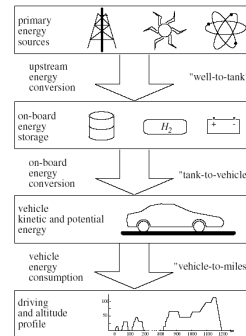
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Losses in the vehicle motion  
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## Energy System Overview



Primary sources

Different options for on-board energy storage

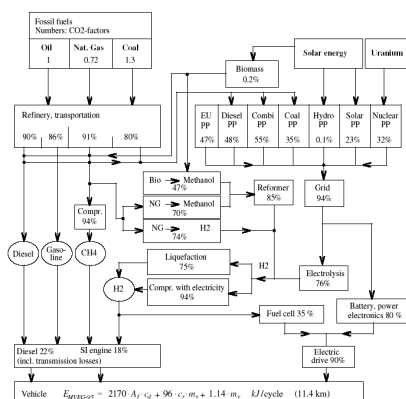
Powertrain energy conversion during driving

Cut at the wheel!

Driving mission has a minimum energy requirement.

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## Example of Some Energy Paths – W2M



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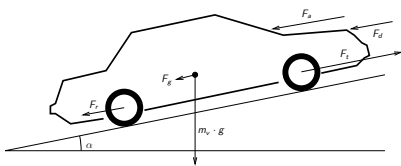
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- ▶ Remember the partitioning  
–Cut at the wheels.
- ▶ How large **force** is required at the wheels for driving the vehicle on a mission?

### The Vehicle Motion Equation

Newton's second law for a vehicle

$$m_v \frac{d}{dt} v(t) = F_t(t) - (F_a(t) + F_r(t) + F_g(t) + F_d(t))$$

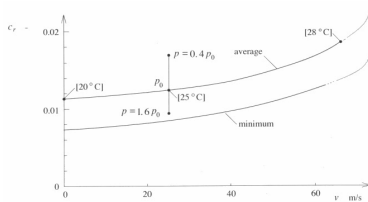


- ▶  $F_t$  – tractive force
- ▶  $F_a$  – aerodynamic drag force
- ▶  $F_r$  – rolling resistance force
- ▶  $F_g$  – gravitational force
- ▶  $F_d$  – disturbance force

### Rolling Resistance Losses

Rolling resistance depends on load and tire/road conditions

$$F_r(v, p_t, \text{surface}, \dots) = c_r(v, p_t, \dots) \cdot m_v \cdot g \cdot \cos(\alpha), \quad v > 0$$

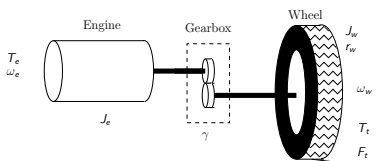


The velocity has small influence at low speeds. Increases for high speeds where resonance phenomena start.

Assumption in book:  $c_r$  – constant

$$F_r = c_r \cdot m_v \cdot g$$

### Inertial forces – Reducing the Tractive Force



$$T_e - J_e \frac{d}{dt} \omega_e = T_{gb} \quad T_{gb} \cdot \gamma - J_w \frac{d}{dt} \omega_w = T_t$$

Variable substitution:  $T_w = \gamma T_e, \quad \omega_w \gamma = \omega_e, \quad v = \omega_w r_w$

Tractive force:

$$F_t = \frac{1}{r_w} \left[ (T_e - J_e \frac{d}{dt} \omega_e) \cdot \gamma - J_w \frac{d}{dt} \omega_w \right] = \frac{\gamma}{r_w} T_e - \left( \frac{\gamma^2}{r_w} J_e + \frac{1}{r_w} J_w \right) \frac{d}{dt} v(t)$$

The Vehicle Motion Equation:

$$\left[ m_v + \frac{\gamma^2}{r_w^2} J_e + \frac{1}{r_w^2} J_w \right] \frac{d}{dt} v(t) = \frac{\gamma}{r_w} T_e - (F_a(t) + F_r(t) + F_g(t) + F_d(t))$$

Translational system – Force, work and power:

$$W = \int F dx, \quad P = \frac{d}{dt} W = F v$$

Rotating system – Torque ( $T = F r$ ), work and power:

$$W = \int T d\theta, \quad P = T \omega$$

Newton's second law:

Translational	Rotational
$m \frac{dv}{dt} = F_{driv} - F_{load}$	$J \frac{d\omega}{dt} = T_{driv} - T_{load}$

### Aerodynamic Drag Force – Loss

Aerodynamic drag force depends on:

Frontal area  $A_f$ , drag coefficient  $c_d$ , air density  $\rho_a$  and vehicle velocity  $v(t)$

$$F_a(t) = \frac{1}{2} \cdot \rho_a \cdot A_f \cdot c_d \cdot v(t)^2$$

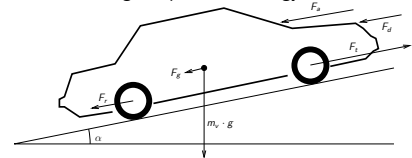
Approximate contributions to  $F_a$

- ▶ 65% car body.
- ▶ 20% wheel housings.
- ▶ 10% exterior mirrors, eave gutters, window housings, antennas, etc.
- ▶ 5% engine ventilation.

### Gravitational Force

- ▶ Gravitational load force

–Not a loss, storage of potential energy



- ▶ Up- and down-hill driving produces forces.

$$F_g = m_v g \sin(\alpha)$$

- ▶ Flat road assumed  $\alpha = 0$  if nothing else is stated (In the book).

### Vehicle Operating Modes

The Vehicle Motion Equation:

$$m_v \frac{d}{dt} v(t) = F_t(t) - (F_a(t) + F_r(t) + F_g(t) + F_d(t))$$

- ▶  $F_t > 0$  traction
- ▶  $F_t < 0$  braking
- ▶  $F_t = 0$  coasting

$$\frac{d}{dt} v(t) = -\frac{1}{2 m_v} \rho_a A_f c_d v^2(t) - g c_r = \alpha^2 v^2(t) - \beta^2$$

Coasting solution for  $v > 0$

$$v(t) = \frac{\beta}{\alpha} \tan \left( \arctan \left( \frac{\alpha}{\beta} v(0) \right) - \alpha \beta t \right)$$

## How to check a profile for traction?

The Vehicle Motion Equation:

$$m_v \frac{d}{dt} v(t) = F_t(t) - (F_a(t) + F_r(t) + F_g(t) + F_d(t)) \quad (1)$$

► Traction conditions:

$F_t > 0$  traction,  $F_t < 0$  braking,  $F_t = 0$  coasting

► Method 1: Compare the profile with the coasting solution over a time step

$$v_{\text{coast}}(t_{i+1}) = \frac{\beta}{\alpha} \tan \left( \arctan \left( \frac{\alpha}{\beta} v(t_i) \right) - \alpha \beta (t_{i+1} - t_i) \right)$$

► Method 2: Solve (1) for  $F_t$

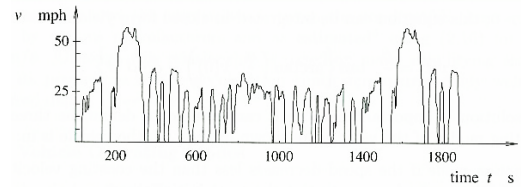
$$F_t(t) = m_v \frac{d}{dt} v(t) + (F_a(t) + F_r(t) + F_g(t) + F_d(t))$$

Numerically differentiate the profile  $v(t)$  to get  $\frac{d}{dt} v(t)$ .  
Compare with [Traction condition](#).

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## Driving profiles

Velocity profile, American FTP-75 (1.5\*FUDS).

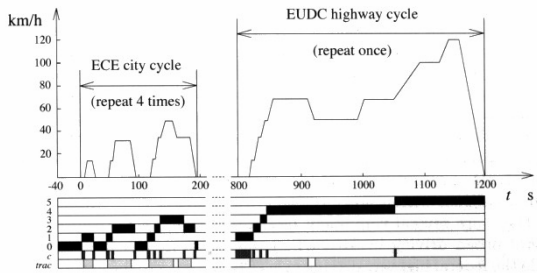


Driving profiles in general

- First used for pollutant control now also for fuel consumption.
- Important that all use the same cycle when comparing.
- Different cycles have different energy demands.

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## Driving profiles – Another example



Velocity profile, European MVEG-95 (ECE\*4, EUDC)

No coasting in this driving profile.

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## Mechanical Energy Demand of a Cycle

**Only** the demand from the cycle

- The mean tractive force during a cycle

$$\bar{F}_{\text{trac}} = \frac{1}{x_{\text{tot}}} \int_0^{x_{\text{tot}}} \max(F(x), 0) dx = \frac{1}{x_{\text{tot}}} \int_{t \in \text{trac}} F(t) v(t) dt$$

where  $x_{\text{tot}} = \int_0^{t_{\text{max}}} v(t) dt$ .

- Note  $t \in \text{trac}$  in definition.
- Only traction.
- Idling not a demand from the cycle.

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## Evaluating the integral

Discretized velocity profile used to evaluate

$$\bar{F}_{\text{trac}} = \frac{1}{x_{\text{tot}}} \int_{t \in \text{trac}} F(t) v(t) dt$$

here  $v_i = v(t_i)$ ,  $t_i = i \cdot h$ ,  $i = 1, \dots, n$ .

Approximating the quantities

$$\bar{v}_i(t) \approx \frac{v_i + v_{i-1}}{2}, \quad t \in [t_{i-1}, t_i]$$

$$\bar{a}_i(t) \approx \frac{v_i - v_{i-1}}{h}, \quad t \in [t_{i-1}, t_i]$$

Traction approximation

$$\bar{F}_{\text{trac}} \approx \frac{1}{x_{\text{tot}}} \sum_{i \in \text{trac}} \bar{F}_{\text{trac},i} \bar{v}_i h$$

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## Evaluating the integral

Tractive force from *The Vehicle Motion Equation*

$$F_{\text{trac}} = \frac{1}{2} \rho_a A_f c_d v^2(t) + m_v g c_r + m_v a(t)$$

$$\bar{F}_{\text{trac}} = \bar{F}_{\text{trac},a} + \bar{F}_{\text{trac},r} + \bar{F}_{\text{trac},m}$$

Resulting in these sums

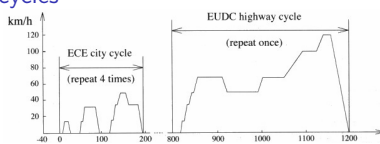
$$\bar{F}_{\text{trac},a} = \frac{1}{x_{\text{tot}}} \frac{1}{2} \rho_a A_f c_d \sum_{i \in \text{trac}} \bar{v}_i^3 h$$

$$\bar{F}_{\text{trac},r} = \frac{1}{x_{\text{tot}}} m_v g c_r \sum_{i \in \text{trac}} \bar{v}_i h$$

$$\bar{F}_{\text{trac},m} = \frac{1}{x_{\text{tot}}} m_v \sum_{i \in \text{trac}} \bar{a}_i \bar{v}_i h$$

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## Values for cycles



Numerical values for the cycles: {MVEG-95, ECE, EUDC}

$$\bar{X}_{\text{trac},a} = \frac{1}{x_{\text{tot}}} \sum_{i \in \text{trac}} \bar{v}_i^3 h = \{319, 82.9, 455\}$$

$$\bar{X}_{\text{trac},r} = \frac{1}{x_{\text{tot}}} \sum_{i \in \text{trac}} \bar{v}_i h = \{0.856, 0.81, 0.88\}$$

$$\bar{X}_{\text{trac},m} = \frac{1}{x_{\text{tot}}} \sum_{i \in \text{trac}} \bar{a}_i \bar{v}_i h = \{0.101, 0.126, 0.086\}$$

$$\bar{E}_{\text{MVEG-95}} \approx A_f c_d 1.9 \cdot 10^4 + m_v c_r 8.4 \cdot 10^2 + m_v 10 \quad \text{kJ/100km}$$

Tasks in Hand-in assignment

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## Approximate car data

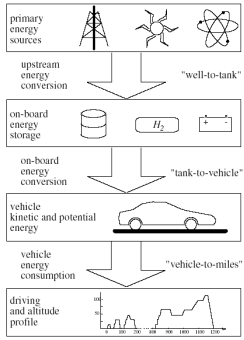
$$\bar{E}_{\text{MVEG-95}} \approx A_f c_d 1.9 \cdot 10^4 + m_v c_r 8.4 \cdot 10^2 + m_v 10 \quad \text{kJ/100km}$$

	SUV	full-size	compact	light-weight	PAC-Car II
$A_f \cdot c_d$	1.2 m <sup>2</sup>	0.7 m <sup>2</sup>	0.6 m <sup>2</sup>	0.4 m <sup>2</sup>	.25 · .07 m <sup>2</sup>
$c_r$	0.017	0.017	0.017	0.017	0.0008
$m_v$	2000 kg	1500 kg	1000 kg	750 kg	39 kg
$\bar{P}_{\text{MVEG-95}}$	11.3 kW	7.1 kW	5.0 kW	3.2 kW	
$\bar{P}_{\text{max}}$	155 kW	115 kW	77 kW	57 kW	

Average and maximum power requirement for the cycle.

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# Energy System Overview



Primary sources

Different options for on-board energy storage

Powertrain energy conversion during driving

Cut at the wheel!

Driving mission has a minimum energy requirement.